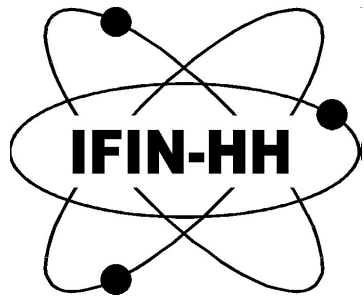


Lecture II.1

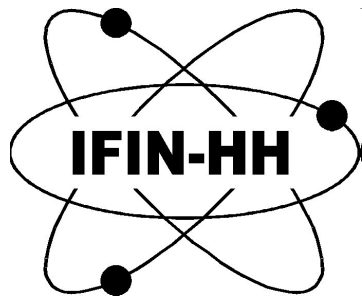
The basics of nuclear reactions

Alexandru Negret

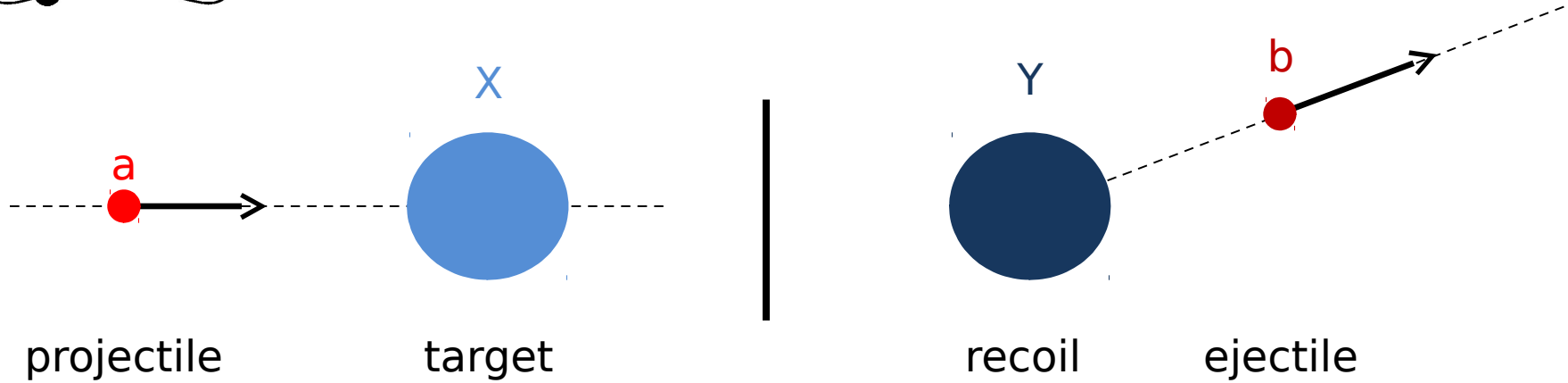


Outline

- Writing a nuclear reaction as $X(a,b)Y$
- Q value
- Coulomb Barrier
- Cross section
- Angular distribution



The Q value

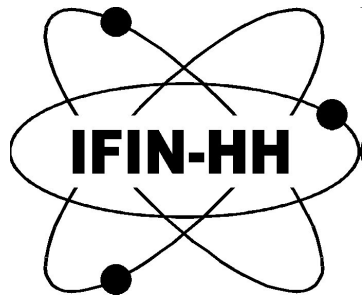


$$m_a^2 c^4 + m_x c^4 = m_y c^4 + m_b c^4$$

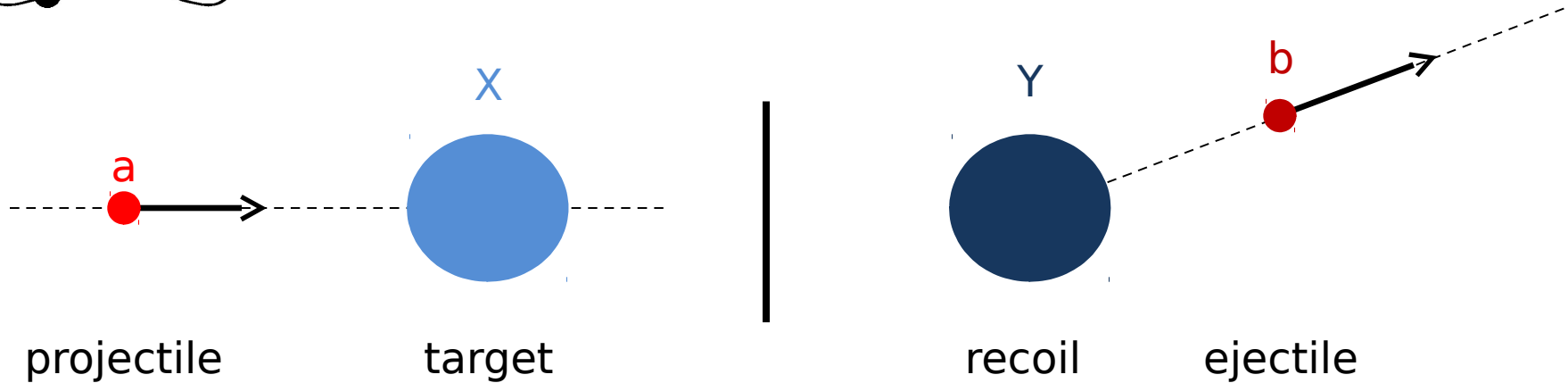
$Q > 0$ exothermal reaction
 $Q < 0$ endothermal reaction

Q-value (reaction energy)





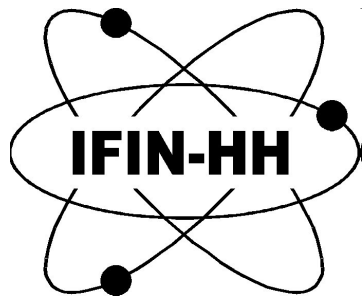
The Coulomb barrier



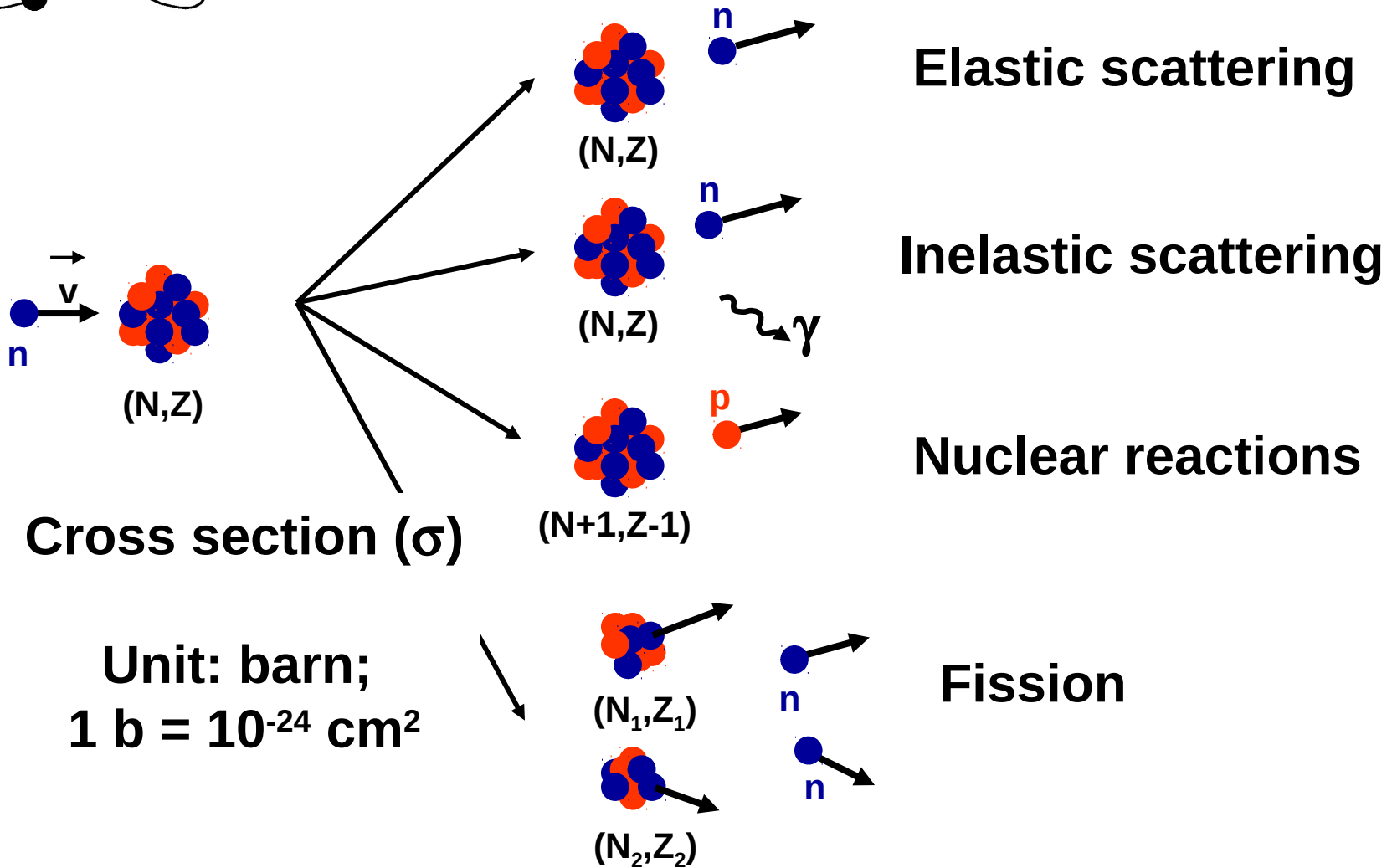
$$V_{Coul} = k \frac{Q_a Q_X}{r} = ke^2 \frac{Z_a Z_X}{r}$$

$$ke^2 = 1.44 \text{ MeV}\cdot\text{fm}$$

$$r = r_0 A^{1/3}; \quad r_0 \approx 1.2 \text{ fm}$$



Cross section



Cross section (σ)

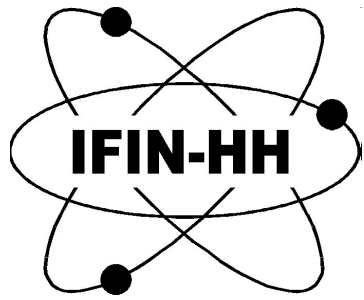
Unit: barn;
1 b = 10^{-24} cm²

Elastic scattering

Inelastic scattering

Nuclear reactions

Fission

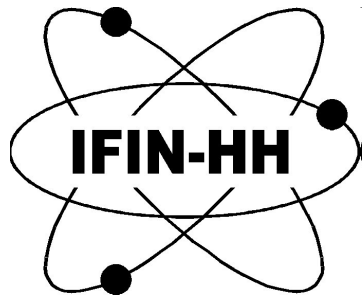


Cross section – the barn

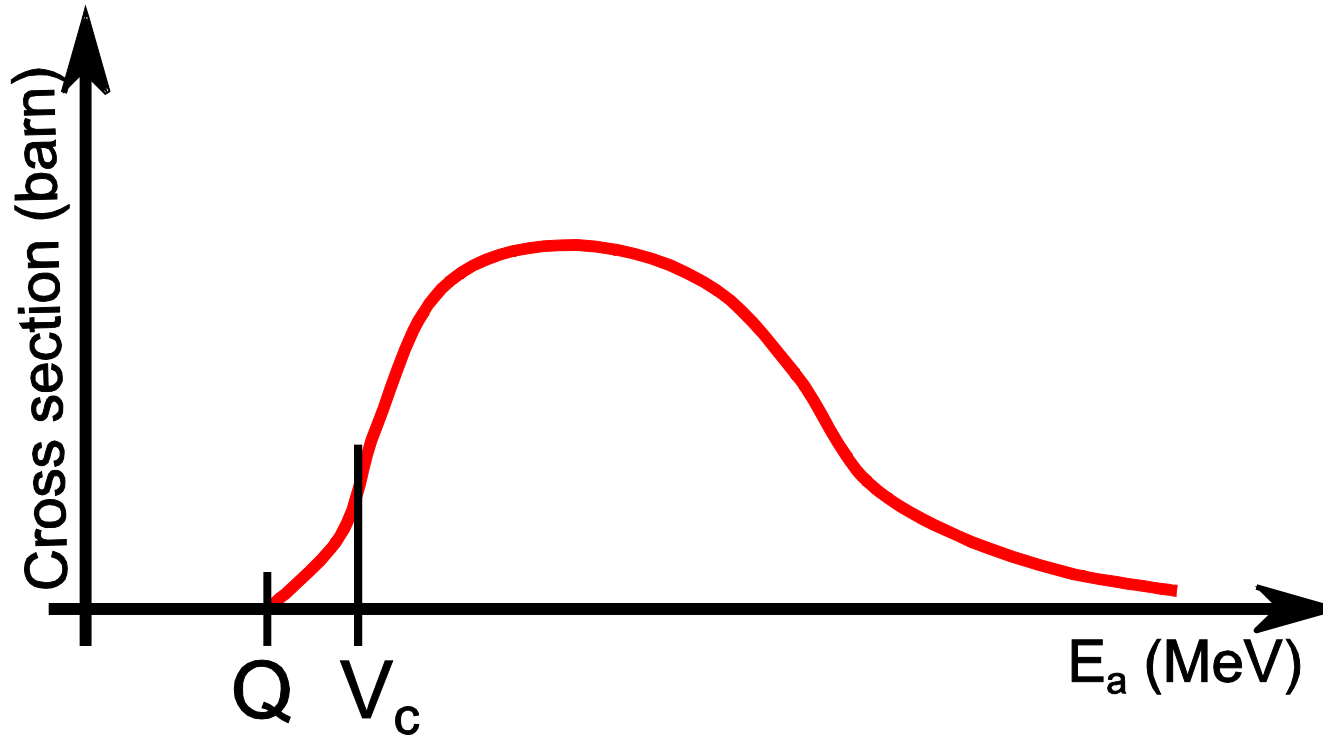
The Uranium nucleus is “big as a barn”.

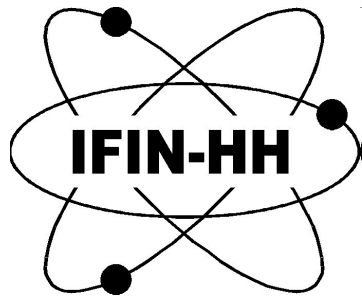


The total cross section $n+^{235}\text{U}$ at $E_n=1$ MeV is ~ 7 b

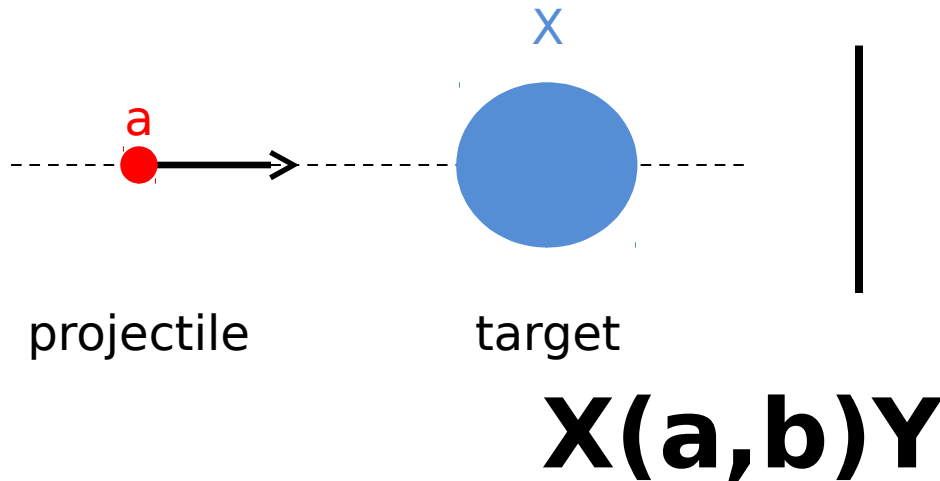


Cross section



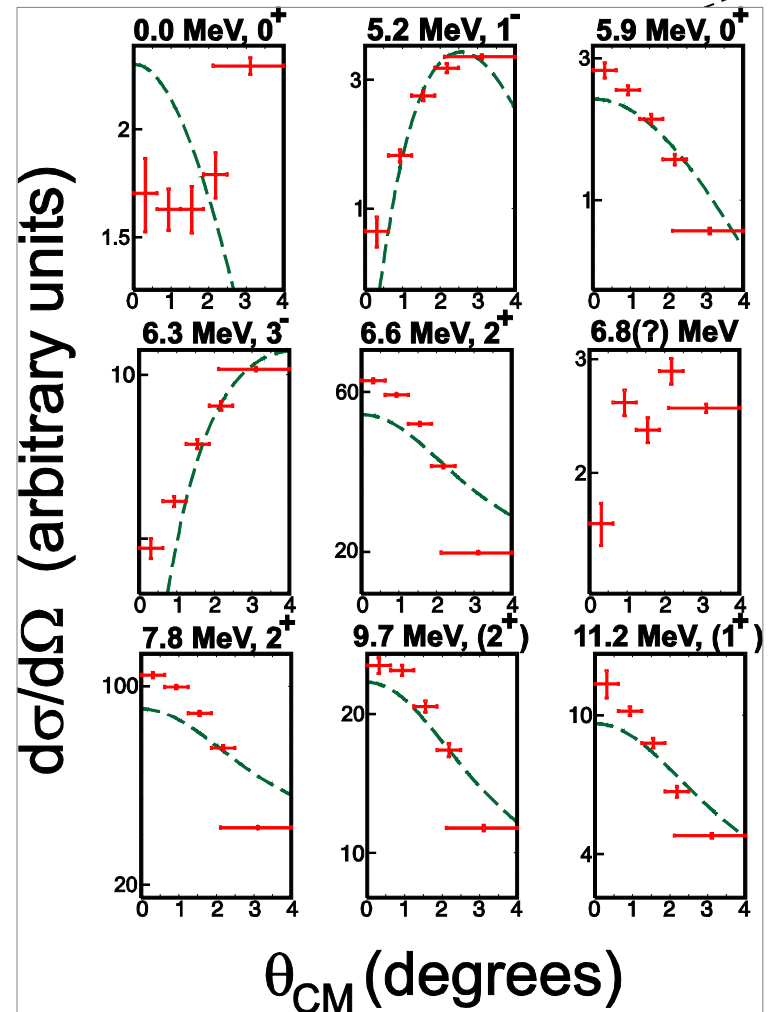


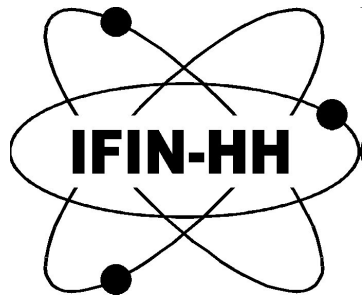
Angular distribution



$$\sigma = \sigma(\theta)$$

The angular momentum transferred determines the angular distribution of the ejectile.





Exercise 1: $^{194}\text{Pt}({}^6\text{Li}, d){}^{198}\text{Hg}$

- Compute Q value

$$m({}^6\text{Li}) = 6.015122 \text{ u}$$

$$m(d) = 2.014102 \text{ u}$$

$$m({}^{194}\text{Pt}) = 193.962681 \text{ u}$$

$$m({}^{198}\text{Hg}) = 197.966769 \text{ u}$$

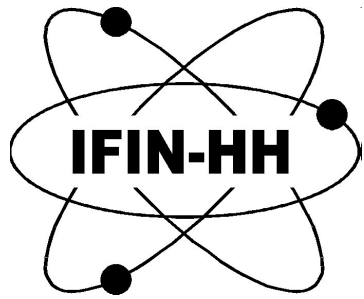
$$uc^2 = 931.5 \text{ MeV}$$

- Compute the Coulomb barrier

$$V_{\text{Coul}} = k \frac{Q_a Q_X}{r} = ke^2 \frac{Z_a Z_X}{r}$$

$$ke^2 = 1.44 \text{ MeV}\cdot\text{fm}$$

$$r = r_0 A^{1/3}; \quad r_0 \approx 1.2 \text{ fm}$$



Exercise 2: $^{28}\text{Si}(n, n')^{28}\text{Si}$

- Compute Q value

$$m(n) = 1.008665 \text{ u}$$

$$m(^{28}\text{Si}) = 27.976926 \text{ u}$$

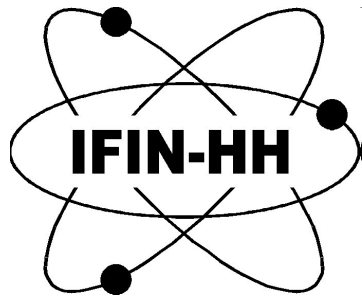
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Summary

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- Q value
- Coulomb Barrier
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